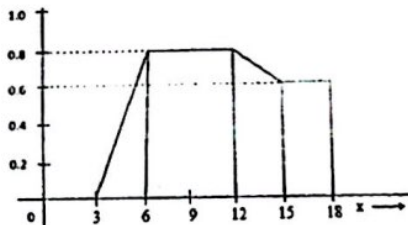


Answer the following questions:

Q1: For the following fuzzy set, find The crisp value which is obtained by CoG, MoM, SoM and LoM. (8 marks)

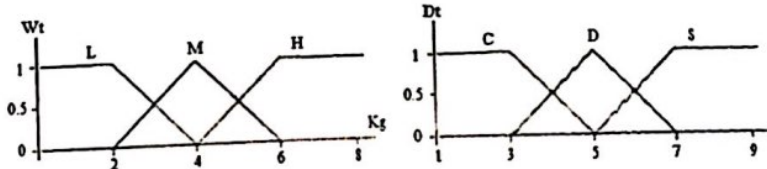


Q2: Let $X=\{1,2,3,4,5\}$ and $Y=\{1,2,3,4,5\}$. The membership functions
 Small = $\{0/1+0.5/2+0/3+0.5/4+1/5\}$, Medium $\{0/1+0.5/2+1/3+0.5/4+0/5\}$, and
 Large = $\{0/1+0.2/2+0.5/3+0.8/4+1/5\}$. The rule-base of the fuzzy logic controller is:

- 1- If x is small Then y is medium
- 2- If x is medium Then y is large
- 3- If x is large Then y is small

Using the fuzzy graph model and max-min method; find the output y if the input:
 $x^* = \{0/1+0.5/2+1/3+0.7/4+0.3/5\}$ (10 marks)

Q3: A controller in washing machine has two inputs; Wt is the weight of clothes (0-8 Kg) with linguistic variables {Light, Medium, Heavy}, and Dt is the amount of dirt {1-9} with linguistic variables {Clean, Dirty, Soiled}, the output Liq is the amount of cleaning liquid in mL {10-200}. The membership function distributions of the controller inputs are shown in the figure below.



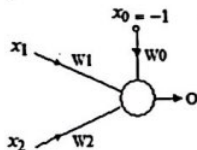
Based on *Sugeno* approach, the rule-base of the fuzzy logic controller is:

- 1- IF Wt is L AND Dt is C THEN Liq = 2 Wt + Dt.
- 2- IF Wt is M OR Dt is D THEN Liq = 6 Wt + 7 Dt + 10.
- 3- IF Wt is M AND Dt is S THEN Liq = 8 Wt + 10 Dt - 6.
- 4- IF Wt is H OR Dt is C THEN Liq = 14 Wt + 16 Dt + 3.
- 5- IF Wt is H AND Dt is D THEN Liq = 18 Wt + 16 Dt + 15.

Find the Output ϕ at Wt = 4.5 Kg and Dt = 4.

{ 10 marks }

Q4: The shown Neural Network has $\alpha=0.2$ and threshold value $\theta = 0$.



This network will be trained to perform AND gate. Find the required weights W0, W1, and W2.

Write the results in the following table:

{ 12 marks }

Epoch	Input			Desired output t	Initial weights			Actual output O	Error e	Final weights		
	x0	x1	x2		w0	w1	w2			w0	w1	w2
1	-1	0	0	0	0.5	1	1					
	-1	0	1	0								
	-1	1	0	0								
	-1	1	1	1								
...	-1	0	0	0								
	-1	0	1	0								
	-1	1	0	0								
	-1	1	1	1								

Final Exam: CT411 (Intelligent Control)
 Answers
 14/03/2022

Q1:

$$A_1 = 3 \times 0.8 \times 0.5 = 1.2$$

$$A_2 = 6 \times 0.8 = 4.8$$

$$A_3 = 3 \times 0.6 = 1.8$$

$$A_4 = 3 \times 0.2 \times 0.5 = 0.3$$

$$A_5 = 3 \times 0.6 = 1.8$$

$$\bar{x}_1 = (3+6)/3 = 5 \quad (0.5)$$

$$\bar{x}_2 = (6+12)/2 = 9 \quad (0.5)$$

$$\bar{x}_3 = (12+15)/2 = 13.5 \quad (0.5)$$

$$\bar{x}_4 = (12+12+15)/3 = 13 \quad (0.5)$$

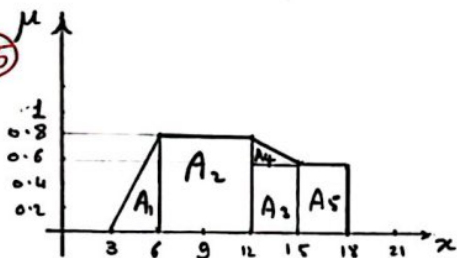
$$\bar{x}_5 = (15+18)/2 = 16.5 \quad (0.5)$$

$$(COG) \quad x^* = \frac{1.2 \times 5 + 4.8 \times 9 + 1.8 \times 13.5 + 0.3 \times 13 + 1.8 \times 16.5}{1.2 + 4.8 + 1.8 + 0.3 + 1.8} = \frac{107.1}{9.9} = 10.82 \quad (2)$$

$$MOM (x^* = \frac{12+6}{2} = 9) \quad (1.5)$$

$$SOM (x^* = 6) \quad (1)$$

$$LoM (x^* = 12) \quad (1)$$



$$Q_2: \quad R_1 = \min \begin{bmatrix} 1 \\ 0.5 \\ 0 \\ 0.5 \\ 1 \end{bmatrix} \circ [0 \ 0.5 \ 1 \ 0.5 \ 0] = \begin{bmatrix} 0 & 0.5 & 1 & 0.5 & 0 \\ 0 & 0.5 & 0.5 & 0.5 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0.5 & 0.5 & 0.5 & 0 \\ 0 & 0.5 & 1 & 0.5 & 0 \end{bmatrix} \quad (1)$$

$$R_2 = \min \begin{bmatrix} 0 \\ 0.5 \\ 1 \\ 0.5 \\ 0 \end{bmatrix} \circ [0 \ 0.2 \ 0.5 \ 0.8 \ 1] = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 0.2 & 0.5 & 0.5 & 0.5 \\ 0 & 0.2 & 0.5 & 0.8 & 1 \\ 0 & 0.2 & 0.5 & 0.5 & 0.5 \\ 0 & 0 & 0 & 0 & 0 \end{bmatrix} \quad (1)$$

$$R_3 = \min \begin{bmatrix} 0 \\ 0.2 \\ 0.5 \\ 0.8 \\ 1 \end{bmatrix} \circ [1 \ 0.5 \ 0 \ 0.5 \ 1] = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0.2 & 0.2 & 0 & 0.2 & 0.2 \\ 0.5 & 0.5 & 0 & 0.5 & 0.5 \\ 0.8 & 0.5 & 0 & 0.5 & 0.8 \\ 1 & 0.5 & 0 & 0.5 & 1 \end{bmatrix} \quad (1)$$

$$R = R_1UR_2UR_3 = \begin{bmatrix} 0 & 0.5 & 1 & 0.5 & 0 \\ 0.2 & 0.5 & 0.5 & 0.5 & 0.5 \\ 0.5 & 0.5 & 0.5 & 0.8 & 1 \\ 0.8 & 0.5 & 0.5 & 0.5 & 0.8 \\ 1 & 0.5 & 1 & 0.5 & 1 \end{bmatrix} \quad (1)$$

$$y^* = \left(\begin{array}{c} \text{max-min} \\ [0 \ 0.5 \ 1 \ 0.7 \ 0.3] \end{array} \begin{bmatrix} 0 & 0.5 & 1 & 0.5 & 0 \\ 0.2 & 0.5 & 0.5 & 0.5 & 0.5 \\ 0.5 & 0.5 & 0.5 & 0.8 & 1 \\ 0.8 & 0.5 & 0.5 & 0.5 & 0.8 \\ 1 & 0.5 & 1 & 0.5 & 1 \end{bmatrix} \right)$$

$$y^*(1,1) = \max(0, 0.2, 0.5, 0.7, 0.3) = 0.7 \quad (1)$$

$$y^*(1,2) = \max(0, 0.5, 0.5, 0.5, 0.3) = 0.5 \quad (1)$$

$$y^*(1,3) = \max(0, 0.5, 0.5, 0.5, 0.3) = 0.5 \quad (1)$$

$$y^*(1,4) = \max(0, 0.5, 0.8, 0.5, 0.3) = 0.8 \quad (1)$$

$$y^*(1,5) = \max(0, 0.5, 1, 0.7, 0.3) = 1 \quad (1)$$

$$y^* = \left\{ \frac{0.7}{1} + \frac{0.5}{2} + \frac{0.5}{3} + \frac{0.8}{4} + \frac{1}{5} \right\}$$

$$CoA(y) = \frac{0.7 \times 1 + 0.5 \times 2 + 0.5 \times 3 + 0.8 \times 4 + 1 \times 5}{0.7 + 0.5 + 0.5 + 0.8 + 1} = \frac{11.4}{3.5} = 3.26 \quad (1)$$

Q₃:

$$F_1 = 2 \times 4.5 + 4 = 13 \quad \left(\begin{array}{c} 0.5 \\ 0.5 \end{array} \right)$$

$$F_2 = 6 \times 4.5 + 7 \times 4 + 10 = 65 \quad \left(\begin{array}{c} 0.5 \\ 0.5 \end{array} \right)$$

$$F_3 = 8 \times 4.5 + 10 \times 4 - 6 = 70 \quad \left(\begin{array}{c} 0.5 \\ 0.5 \end{array} \right)$$

$$F_4 = 14 \times 4.5 + 16 \times 4 + 3 = 130 \quad \left(\begin{array}{c} 0.5 \\ 0.5 \end{array} \right)$$

$$F_5 = 18 \times 4.5 + 16 \times 4 + 15 = 160 \quad \left(\begin{array}{c} 0.5 \\ 0.5 \end{array} \right)$$

Q4:

Epoch	Inputs			Desired output	Inputs			Actual output	Δw			Final weights			
	x_0	x_1	x_2	t	w_0	w_1	w_2	O	e	Δw_0	Δw_1	Δw_2	w_0	w_1	w_2
1	-1	0	0	0	0.5	1	1	-0.5	0	0	0	0	0.5	1	1
	-1	0	1	0	0.5	1	1	0.5	1	-1	0.2	-0.2	0.7	1	0.8
	-1	1	0	0	0.7	1	0.8	0.3	1	-1	0.2	-0.2	0.9	0.8	0.8
2	-1	1	1	1	0.9	0.8	0.8	0.7	1	0	0	0	0.9	0.8	0.8
	-1	0	0	0	0.9	0.9	0.8	-0.9	0	0	0	0	0.9	0.8	0.8
	-1	0	1	0	0.9	0.9	0.7	-0.1	0	0	0	0	0.9	0.8	0.8
3	-1	1	0	0	0.9	0.9	0.7	-0.1	0	0	0	0	0.9	0.8	0.8
	-1	1	1	1	0.9	0.9	0.7	0.7	1	0	0	0	0.9	0.8	0.8
	-1	1	1	1	0.9	0.8	0.7	0.7	1	0	0	0	0.9	0.8	0.8

$$O = w_0 x_0 + w_1 x_1 + w_2 x_2$$

$$\Delta w_i = \alpha (t_i - O_i) x_i$$

1.5
1.5
1.5
1.5
1.5
1.5
1.5
1.5